

# Math: Operations and Algebraic Thinking: Represent and Solve Problems

## Students: DesCartes Statements:

### Students:

#### RIT Above 250:

- Uses reasoning strategies to solve problems

### Students:

#### RIT 241-250:

- Applies algebraic methods to solve real-world problems
- Solves multiple-step problems involving proportions
- Uses reasoning strategies to solve problems

### Students:

#### RIT 231-240:

- Applies algebraic methods to solve real-world problems
- Evaluates numerical expressions using the order of operations (whole numbers only)
- Models algorithms using place value concepts (multiplication and division with whole numbers)
- Represents relationships of quantities in the form of an expression
- Solves multiple-step problems involving proportions
- Solves problems comparing unit prices
- Uses pictures to represent problems

### Students:

#### RIT 221-230:

- Applies algebraic methods to solve real-world problems
- Applies algebraic methods to solve theoretical problems
- Demonstrates an understanding of multiple properties
- Models algorithms using place value concepts (multiplication and division with whole numbers)
- Represents relationships of quantities in the form of an expression
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves open sentences with calculations on both sides of the sentence
- Solves real-world multiple-step problems involving whole numbers
- Uses multiple number theory concepts to solve problems (e.g., factors, digits, odd/even, divisibility)
- Uses pictures to represent problems
- Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)

### Students:

#### RIT 211-220:

- Applies algebraic methods to solve theoretical problems
- Demonstrates an understanding of the associative property of multiplication
- Demonstrates an understanding of the commutative property of multiplication with simple problems
- Demonstrates an understanding of the distributive property of multiplication by decomposing a term
- Demonstrates an understanding of the inverse relationship between addition and subtraction
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Performs mental computation with division
- Predicts the relative size of the answer when multiplying whole numbers
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves open sentences using the distributive property
- Solves open sentences with calculations on both sides of the sentence
- Solves real-world multiple-step problems involving whole numbers
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves simple open sentences with missing factors (numbers over 100)
- Solves whole number word problems with division over  $10 \times 10$
- Translates a 2-step problem to a symbolic expression or equation
- Understands equivalence and extends the concept to number sentences involving variables (e.g.,  $8 + 2 = [] + 2$ )
- Uses algebraic reasoning to solve problems involving equality relationships
- Uses pictures to represent problems
- Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses simple linear equations to represent problem situations

**Students:****RIT 201-210:**

- Demonstrates an understanding of the commutative property of multiplication with simple problems
- Describes a realistic situation using information given in a linear equation
- Determines the remainder in a real-world problem (whole numbers)
- Evaluates numerical expressions using grouping symbols (whole numbers only)
- Instantly recalls division facts with dividend and divisors less than 13
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Performs mental computation with division
- Solves 2-step open sentences with missing addends
- Solves open sentences with basic-facts calculations on both sides of the sentence
- Solves problems using tables
- Solves problems using the inverse relationship between addition and subtraction
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves real-world whole number problems involving subtraction with numbers 100 and under (analysis)
- Solves simple open sentences with missing factors (numbers 100 and under)
- Solves simple word problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor)
- Solves whole number subtraction word problems with numbers over 1000
- Solves whole number word problems with division over  $10 \times 10$
- Solves word problems involving whole number multiplication with numbers greater than  $10 \times 10$
- Solves word problems with whole number division facts with dividend and divisors less than 11
- Translates a 1-step problem to a symbolic expression or equation
- Translates a 2-step problem to a symbolic expression or equation
- Understands equivalence and extends the concept to number sentences involving variables (e.g.,  $8 + 2 = \square + 2$ )
- Uses algebraic reasoning to solve problems involving equality relationships
- Uses division for multiple-step real-world problems (whole numbers)
- Uses number sense strategies to solve problems (addition/subtraction only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only)
- Uses simple linear equations to represent problem situations

**Students:****RIT 191-200:**

- Demonstrates an understanding of the commutative property of multiplication with simple problems
- Demonstrates an understanding of the zero property of multiplication
- Determines the operation needed from a simple problem
- Distinguishes between odd and even numbers
- Evaluates numerical expressions using grouping symbols (whole numbers only)
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12
- Instantly recalls division facts with dividend and divisors less than 10
- Instantly recalls division facts with dividend and divisors less than 13
- Interprets a chart or table - calculation required
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Solves 1-step open sentences with missing addends (numbers 100 and under)
- Solves 2-step open sentences with missing addends
- Solves problems using tables
- Solves problems using the inverse relationship between addition and subtraction
- Solves real-world whole number addition problems with sums to 20 (change unknown)
- Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given
- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves real-world whole number problems involving subtraction with numbers under 1000
- Solves simple open sentences with missing factors (numbers 100 and under)
- Solves simple word problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor)
- Solves whole number subtraction word problems with numbers over 1000
- Solves word problems involving basic whole number multiplication facts to  $10 \times 10$
- Solves word problems involving whole number multiplication with numbers greater than  $10 \times 10$
- Solves word problems with whole number division facts with dividend and divisors less than 11
- Translates a 1-step problem to a symbolic expression or equation
- Uses algebraic reasoning to solve problems involving equality relationships
- Uses manipulatives to divide a small set of objects into groups of equal size
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with addition and subtraction (whole numbers only)
- Writes equivalent forms of whole numbers 11 to 20 using addition (e.g.,  $14 = 7 + 7$ )

**Students:****RIT 181-190:**

- Demonstrates an understanding of the inverse relationship between multiplication and division
- Demonstrates an understanding of the zero property of multiplication
- Determines the operation needed from a simple problem
- Distinguishes between odd and even numbers
- Instantly recalls basic addition facts with sums to 18 in a table
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12
- Instantly recalls basic subtraction facts with minuend less than 10
- Instantly recalls division facts with dividend and divisors less than 10
- Interprets a chart or table - calculation required
- Models multiplication and division algorithms using arrays (whole numbers)
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Multiplies basic facts to 10 x 10 vertically
- Recognizes addition and subtraction fact families through 18
- Solves 1-step open sentences with missing addends (numbers 100 and under)
- Solves basic facts addition and subtraction open sentences using diagrams and models (e.g., using balances)
- Solves problems using the inverse relationship between addition and subtraction
- Solves real-world whole number addition problems with sums to 100 (result unknown)
- Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given
- Solves real-world whole number problems involving addition and subtraction
- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves real-world whole number problems involving subtraction with numbers under 1000
- Solves real-world whole number problems involving subtraction with numbers under 20
- Solves word problems involving basic whole number multiplication facts to 10 x 10
- Uses counting by multiples for multiplication
- Uses manipulatives to divide a small set of objects into groups of equal size
- Uses rounding to estimate answers to real-world problems involving addition of numbers less than 100 (whole numbers only)
- Uses sharing for division
- Writes a number sentence for a simple problem solving situation
- Writes equivalent forms of whole numbers 11 to 20 using addition (e.g.,  $14 = 7 + 7$ )

**Students:****RIT 171-180:**

- Adds 1-digit numbers with sums to 18 (with parentheses)
- Counts by 2's to 100
- Determines the operation needed from a simple problem
- Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12
- Multiplies basic facts to 10 x 10 vertically
- Recognizes addition and subtraction fact families through 18
- Represents a basic facts addition problem with a number sentence
- Solves basic facts open sentences - multiplication and division
- Solves basic-facts open sentences - addition and subtraction
- Solves real-world whole number addition problems with sums to 100 (result unknown)
- Solves real-world whole number addition problems with sums to 20 (result unknown)
- Solves real-world whole number addition problems with sums to 20 (start unknown)
- Solves real-world whole number problems involving subtraction with numbers under 20
- Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only)
- Uses a number line to construct addition facts with sums through 20 (whole numbers)
- Writes a number sentence for a simple problem solving situation
- Writes equivalent forms of whole number expressions (e.g.,  $15 + 5 = 10 + 10$ )

**Students:****RIT 161-170:**

- Adds two 1-digit numbers with sums between 10 and 19 in horizontal format
- Adds two 1-digit numbers with sums between 10 and 19 in vertical format
- Adds two 1-digit numbers with sums to 10 in horizontal format
- Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12
- Solves basic-facts open sentences - addition and subtraction
- Solves real-world whole number addition problems with sums to 20 (result unknown)
- Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only)
- Subtracts two 1-digit numbers vertically
- Uses a number line to construct addition facts with sums through 20 (whole numbers)

**Students:**

**RIT Below 161:**

- Adds two 1-digit numbers with sums to 10 in horizontal format
- Uses models to construct whole number addition facts with addends through 10