Math: The Real and Complex Number Systems: Perform Operations

Students:	DesCartes Statements:
Students:	 RIT Above 260: Performs operations on complex numbers and expresses the results in simplest form
Students:	 RIT 251-260: Performs operations on complex numbers and expresses the results in simplest form Uses factor and multiple concepts to solve difficult problems Uses the additive inverse property with rational numbers
Students:	 RIT 241-250: Identifies the least common multiple of whole numbers Subtracts integers Uses a number line to determine the distance between a positive and negative number Uses factor and multiple concepts to solve difficult problems Uses the multiplicative inverse property with rational numbers
Students:	 RIT 231-240: Adds fractions with unlike denominators with reducing or converting to a mixed fraction Adds mixed fractions where converting from improper fractions is necessary Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths) Divides a decimal by 0, 100, 100 Divides a decimal by 0 mixed fraction Divides a fraction by a whole number Divides a mixed fraction by a fraction Divides a mixed fraction by a whole number Divides a mixed fraction by a whole number Divides a mixed fraction by a whole number Divides a whole number by a decimal Divides a whole number by a decimal Divides a whole number by a fraction Divides a whole number by a noixed fraction Divides a whole number by a noixed fraction Divides integers with like signs Divides integers with like signs Divides numbers by powers of 10 Identifies the additive inverse property Interprets data given in tables to solve problems Multiplies rational expressions Solves 2- or more step real-world problems involving fractions with multiplication and division Solves problems involving fractions (e.g., multiple operations, conversions) Solves real-world problems involving addition and subtraction of fractions where converting both denominators is necessary Subtracts a decimal from a whole number,

Students:	RIT 221-230:
	Adds decimals through the hundred-thousandths place
	 Adds decimals to the hundredths place in horizontal format (not same number of digits)
	 Adds fractions with like denominators with reducing or converting to a mixed fraction
	 Adds fractions with unlike denominators with reducing or converting to a mixed fraction
	Adds fractions with unlike denominators without reducing
	Adds integers with unlike signs
	 Adds mixed fractions where converting from improper fractions is necessary
	Adds rational expressions in decimal form
	Adds several positive and negative integers
	Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
	Calculate the sum of integers using a number line
	Computes the value of multiple bills and coins (multiplication/division)
	Computes with dollars and cents over \$5.00 and converts to decimals (multiplication/division)
	Demonstrates an understanding of multiple properties
	Determines factors of whole numbers
	Divides a 4-digit number by a 2-digit number
	Divides a decimal by 10, 100, 1000
	Divides a decimal by a decimal
	Divides a fraction by a fraction
	Divides a mixed fraction by a fraction
	Divides integers with like signs
	Divides integers with unlike signs
	Divides multiple-digit numbers
	Identifies the additive inverse preperty
	Identifies the greatest common factor of whole numbers
	Interprets data given in tables to solve problems
	Multiplies a decimal by 10, 100, 1000
	Multiplies a decimal by rol root Multiplies a decimal by a decimal (factors to hundredths)
	Multiplies a decimal by a decimal (factors to thousandths)
	Multiplies a decimal by a decimal (accors to threadenedis)
	Multiplies a fraction by a fraction where reducing to simplest form is necessary
	Multiplies a fraction by a fraction without reducing to simplest form (complex problem)
	Multiplies a fraction by a whole number
	Multiplies integers with unlike signs
	Multiplies mixed fractions
	Multiplies multiple-digit numbers
	Solves 1-step real-world problems involving fractions with multiplication and division
	Solves 2- or more step real-world problems involving fractions with multiplication and division
	• Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
	Solves difficult problems involving elapsed time, with the conversion of hours
	Solves problems involving addition and subtraction of integers
	Solves problems involving fractions (e.g., multiple operations, conversions)
	 Solves real-world multiple-step problems involving whole numbers
	Solves real-world problems involving addition and subtraction of fractions where converting one
	denominator is necessary
	 Solves real-world problems involving addition and subtraction of integers
	Subtracts a decimal from a whole number, horizontally
	Subtracts decimals through the hundred-thousandths place, horizontally
	Subtracts decimals to the hundredths place (not same number of digits)
	Subtracts decimals to the thousandths place, horizontally, with and without regrouping
	Subtracts fractions with like denominators with reducing
	Subtracts fractions with unlike denominators with reducing
	Subtracts fractions with unlike denominators without reducing
	Subtracts integers
	Subtracts mixed fractions with unlike denominators with no regrouping
	Subtracts whole numbers, tractions, and mixed fractions
	Subtracts whole numbers, inactions, and mixed fractions with regrouping
	Uses models to add and subtract integers and connect the actions to algorithms
	Uses models to multiply and divide fractions and connect the actions to algorithms
	oses models to multiply and divide nactions and connect the actions to algorithms

	 Uses multiple number theory concepts to solve problems (e.g., factors, digits, odd/even, divisibility) Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only) Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only) Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only) Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only) Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10 Writes a simple mixed fraction as a decimal and vice versa
Students:	RIT 211-220:
	Adds decimals through the hundred-thousandths place
	 Adds decimals to the hundredths place in horizontal format (not same number of digits)
	Adds decimals to the thousandths place horizontally with and without regrouping
	Adds fractions with like denominators with reducing or converting to a mixed fraction
	Adds fractions with unlike denominators without reducing
	Adds integers with like signs
	 Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
	 Analyzes and computes 1 operation on real-world problems involving money over \$5.00 (addition/subtraction only)
	 Analyzes and computes 1 operation on real-world problems involving money over \$5.00 (multiplication/division)
	Computes addition and subtraction on multiple-step real-world problems involving money
	Computes addition, subtraction, multiplication, and division on multiple-step, real-world problems involving money
	Computes the value of multiple bills and coins (addition/subtraction only) Computes with dollars and cents over \$5,00 and converts to decimals (multiplication/division)
	Demonstrates an understanding of the inverse relationship between addition and subtraction
	 Demonstrates an understanding that division by o is undefined
	Determines factors of whole numbers
	Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder
	Divides a 3-digit number by a 2-digit number
	Divides a 4-digit number by a 1-digit number with no remainder
	Divides a 4-digit number by a 2-digit number
	Divides decimal by a whole number Divides integers with like signs
	Divides integers with unlike signs
	Divides multiple-digit numbers
	Expresses a percent as a decimal and vice versa
	• Expresses a simple fraction as a decimal
	Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)
	Identifies common factors of two or more numbers
	Identifies numbers as prime
	Identifies the greatest common factor of whole numbers Instantly recalls basis multiplication and division factor in a table
	 Instantly recalls basic multiplication and division facts in a table Models whole number multiplication and division algorithms (o.g., uses physical materials to show 4 groups)
	of a objects)
	 Multiplies a 2-digit number by a 2-digit number with regrouping
	Multiplies a 3-digit number by a 2-digit number with regrouping
	Multiplies a 3-digit number by a 3-digit number
	Multiplies a 4- or more digit number by multiples of 100 or 1000
	Multiplies a decimal by a decimal (factors to hundredths)
	Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
	Multiplies a fraction by a fraction where reducing to simplest form is necessary Multiplies a fraction by a whole number
	Multiplies integers with unlike signs
	Multiplies multiple-digit numbers
	Performs mental computation with division
	Performs mental computation with multiplication
	Selects and uses the appropriate units depending on degree of accuracy required to solve problems
	Solves 1-step real-world problems involving fractions with multiplication and division

•	Solves difficult	problems	involving	elapsed ti	me, with the	conversion	of hours
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- Solves real-world multiple-step problems involving whole numbers
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Solves real-world problems involving addition and subtraction of integers
- Solves whole number word problems with division over 10 x 10
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Subtracts fractions with unlike denominators without reducing
- Subtracts mixed fractions with like denominators with no regrouping
- Subtracts mixed fractions with unlike denominators with no regrouping
- Subtracts numbers with 5 digits or more with regrouping
- Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)
- Uses models to add and subtract integers and connect the actions to algorithms
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Uses multiplication strategies to explain computation (e.g., doubles, 9-patterns, decomposing, partial products)
- Uses rounding to estimate answers to difficult multiplication and division problems (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10
- Writes a simple mixed fraction as a decimal and vice versa

Students:	RIT 201-210:
Statents	 Adds decimals to the thousandths place horizontally with and without regrouping
	Adds fractions with like denominators without reducing
	Adds multiple-digit numbers with sums under 1000
	Adds multiple-digit numbers, with regrouping, with sums over 1000
	Adds whole numbers and fractions
	 Computes addition and subtraction on multiple-step real-world problems involving money
	Computes addition, subtraction, multiplication, and division on multiple-step, real-world problems involving money
	Computes money problems with multiple operations (addition/subtraction only)
	Computes the value of multiple bills and coins (addition/subtraction only)
	• Computes with dollars and cents up to and including \$5.00 and converts to decimals (multiplication/division)
	Determines the remainder in a real-world problem (whole numbers)
	Divides a 2-digit number by a 1-digit number with no remainder
	 Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder
	Divides a 3-digit number by a 1-digit number with no remainder
	Divides a 3-digit number by a multiple of 10
	Divides a 4-digit number by a 1-digit number with no remainder
	Divides a 4-digit number by a 2-digit number
	Divides decimal by a whole number
	 Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)
	 Instantly recalls basic multiplication and division facts in a table
	 Instantly recalls division facts with dividend and divisors less than 13
	 Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
	Multiplies a 2- or 3-digit number by multiples of 10 or 100
	 Multiplies a 2-digit number by a 1-digit number with regrouping
	 Multiplies a 2-digit number by a 2-digit number with regrouping
	Multiplies a 3- or 4-digit number by a 1-digit number
	 Multiplies a 3-digit number by a 2-digit number with regrouping
	Multiplies a 3-digit number by a 3-digit number
	Multiplies a decimal by whole number
	 Multiplies a fraction by a fraction without reducing to simplest form (simple problem)
	Multiplies multiple 1-digit numbers
	Performs mental computation with division
	Performs mental computation with more than 4 addends

	 Performs mental computation with multiplication Solves problems involving measurement of time Solves problems using tables Solves problems using the inverse relationship between addition and subtraction Solves real-world 1-step problems involving 2-step multiple operations, whole numbers only Solves real-world problems involving addition and subtraction of fractions with like denominators Solves real-world problems involving addition and subtraction of integers Solves real-world whole number problems involving subtraction of hours Solves simple problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor) Solves word problems involving whole number multiplication with numbers greater than 10 x 10 Solves word problems with whole number division facts with dividend and divisors less than 11 Subtracts 3- or 4-digit numbers with regrouping Subtracts decimals to the hundred-thousandths place, vertically Subtracts decimals to the hundred splace (same number of digits) with regrouping Subtracts fractions with like denominators with no regrouping Subtracts mixed fractions with like denominators with no regrouping Subtracts numbers with 5 digits or more with regrouping Uses rounding to estimate answers to addition and subtraction problems (whole numbers) Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only) Writes a terminating decimal as a fraction or mixed number
Students:	 RIT 191-200: Adds decimals to the hundredths place (same number of digits) Adds decimals to the hundredths place in vertical format (not same number of digits) Adds money with regrouping Adds multiple-digit numbers, with sums under 1000 Adds multiple-digit numbers, with regrouping, with sums over 1000 Adds multiple-digit numbers, with regrouping, with sums over 1000 Adds multiple-digit numbers, with regrouping, with sums over 1000 Adds two 3- and/or 4-digit numbers, with regrouping, with sums over 1000 Computes 1 operation on real-world problems involving money over \$5.00 (addition/subtraction only) Computes 1 operation on real-world problems involving money over \$5.00 (multiplication/division) Computes basic operations with units of weight/mass Computes with dollars and cents up to and including \$5.00 and converts to decimals (addition/subtraction only) Computes with dollars and cents up to and including \$5.00 and converts to decimals (multiplication/division) Determines elapsed clock time Determines lapsed clock time Determines the operation needed from a simple problem Distinguishes between odd and even numbers Divides a 2-digit number by a 1-digit number with no remainder Finds equivalent combinations of coins with the same value Identifies the value of a collection of coins to \$1.00 (without picture of coins) Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12 Instantly recalls division facts with dividend and divisors less than 13 Makes change to \$1.00 by "counting on" or subtracting Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division algorithms (e.g., shows multiplication as repeated addition and division algorithm to regrouping Multiplies a 2-digit number by a
	 Multiplies a 3- or 4-digit number by a 1-digit number Multiplies a decimal by whole number

Performs mental computation with multiplication

- Performs mental subtraction with numbers under 1000
- Solves problems using tables
- Solves problems using the inverse relationship between addition and subtraction
- Solves real-world 1-step problems involving addition and subtraction of fractions with like denominators
- Solves real-world 1-step problems involving multiplication or division of a whole number by a fraction
- Solves real-world problems involving decimals (not money) using addition and subtraction
- Solves real-world whole number addition problems with sums to 20 (change unknown)
- Solves real-world whole number addition problems with sums to 20 (result unknown) with extraneous
 information given
- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves simple problems involving elapsed time, with the conversion of hours
- Solves simple word problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor)
- Solves whole number addition word problems with sums over 1000
- Solves word problems involving basic whole number multiplication facts to 10 x 10
- Solves word problems involving whole number multiplication with numbers greater than 10 x 10
- Solves word problems with whole number division facts with dividend and divisors less than 11
- Subtracts 1-digit number from a 2-digit number with regrouping
- Subtracts 3- or 4-digit numbers with regrouping
- Subtracts a 2-digit number from a 2-digit number, with regrouping
- Subtracts a 2-digit number from a 3-digit number with a single regrouping
- Subtracts decimals to the hundredths place (same number of digits) with regrouping
- Subtracts decimals to the thousandths place, vertically, with and without regrouping
- Subtracts fractions with like denominators without reducing
- Subtracts multiple-digit numbers with no regrouping
- Tells time to the nearest 1 minute
- Tells time to the nearest quarter hour
- Uses manipulatives to divide a small set of objects into groups of equal size
- Uses models to add and subtract fractions and connect the actions to algorithms
- Uses rounding to estimate answers to addition and subtraction problems (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with addition and subtraction (whole numbers only)
- Uses strategies for sums and differences with 2-digit numbers (e.g., decomposing, compatible, compensation, partial sums, counting on)

RIT 181-190: Students: • Adds 3-digit numbers, with regrouping, with sums under 1000 • Adds decimals to the hundredths place (same number of digits) • Adds money with regrouping • Adds multiple-digit numbers, with regrouping, with sums over 1000 Adds two 3- and/or 4-digit numbers, with regrouping, with sums over 1000 • Adds two or three 2-digit number with regrouping Combines a collection of coins and identifies the correct notation Computes 1 operation on addition or subtraction real-world problems involving money up to \$5.00 Computes with dollars and cents up to and including \$5.00 and converts to decimals (addition/subtraction only) Demonstrates an understanding of the inverse relationship between multiplication and division Determines elapsed clock time Determines elapsed time involving whole hours, whole days, whole years Determines elapsed time under 1 hour or to the hour Determines the operation needed from a simple problem Distinguishes between odd and even numbers Finds equivalent combinations of coins with the same value Identifies the correct time, given the words, and vice versa • Identifies the number that is "1 less than" a given number • Identifies the value of a collection of coins and bills to \$10.00 by "counting on" (with picture of money) • Identifies the value of a collection of coins to \$1.00 (without picture of coins) • Instantly recalls basic addition facts with sums to 18 in a table Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12 Instantly recalls basic subtraction facts with minuend less than 10 Instantly recalls division facts with dividend and divisors less than 10 • Makes change to \$1.00 by "counting on" or subtracting Models multiplication and division algorithms using arrays (whole numbers) Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition •

	 and division as repeated subtraction) Multiplies a 2-digit number by a 1-digit number with regrouping Multiplies a 2-digit number by a 2-digit number with no regrouping Multiplies basic facts to 10 x 10 vertically Performs mental computation with 2, 3, or 4 addends Performs mental subtraction with numbers under 1000 Recognizes addition and subtraction fact families through 18 Solves problems using the inverse relationship between addition and subtraction Solves real-world whole number addition problems with sums to 100 (result unknown) Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given Solves real-world whole number problems involving addition and subtraction Solves real-world whole number problems involving subtraction with numbers 100 and under Solves real-world whole number problems involving subtraction with numbers 100 and under Solves real-world whole number problems involving subtraction with numbers under 20 Solves real-world whole number problems involving subtraction facts to 10 x 10 Subtracts 2- and/or 3-digit numbers with no regrouping Subtracts 3 - or 4-digit numbers with regrouping Subtracts 3 - or 4-digit numbers with regrouping Subtracts autiple-digit numbers with no regrouping Uses counting by multiples for multiplication Uses counting by multiples for multiplication Uses rounding to estimate answers to real-world problems
Students:	RIT 171-180: Adds 1- and/or 2-digit numbers with sums under 100 Adds 1-digit numbers with sums to 18 (with parentheses) Adds 3-digit numbers with no regrouping Adds 3-digit numbers, with regrouping, with sums under 1000 Adds two or three 2-digit number with regrouping Connects money with place value Determines the operation needed from a simple problem Identifies the value of a collection of coins and bills to \$10.00 by "counting on" (with picture of money) Identifies the value of a collection of coins to \$1.00 (with pictures of coins) Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12 Multiplies basic facts to 10 x 10 vertically Recognizes addition and subtraction fact families through 18 Solves real-world whole number addition problems with sums to 100 (result unknown) Solves real-world whole number addition problems with sums to 20 (result unknown) Solves real-world whole number addition problems with sums to 20 (result unknown) Solves real-world whole number addition problems with sums to 20 (start unknown) Solves real-world whole number addition problems with sums to 20 (whole numbers only) Subtracts 2- and/or 3-digit numbers with no regrouping Subtracts a 1-digit number from a 2-digit number with no regrouping, vertically Subtracts a 1-digit number from a 2-digit number with no regrouping Tells time to the nearest 5 minutes Tells time to the nearest 5 minutes Tells time to the nearest fall hour Tells time to the nearest hour Uses a number line to construct addition facts with sums through 20 (whole numbers) Uses models to calculate whole number sums through 99 Uses models to calculate whole number sums through 99 Uses models to calculate whole number sums through 99
Students:	 RIT 161-170: Adds 1-digit to multiple-digit number with no regrouping Adds 1-digit to multiple-digit number with regrouping Adds 2-digit numbers with no regrouping
	 Adds multiple 1-digit numbers Adds two 1-digit numbers with sums between 10 and 19 in horizontal format

	 Adds two 1-digit numbers with sums between 10 and 19 in vertical format Adds two 1-digit numbers with sums to 10 in horizontal format Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12 Solves real-world whole number addition problems with sums to 20 (result unknown) Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only) Subtracts a 2-digit number from a 2-digit number, with no regrouping Subtracts two 1-digit numbers horizontally Subtracts two 1-digit numbers vertically Tells time to the nearest half hour Tells time to the nearest hour Uses a number line to construct addition facts with sums through 20 (whole numbers) Uses models to calculate whole number sums through 99 Uses strategies for addition facts (e.g., compatible numbers, counting on, doubles, neighbors, making tens)
Students:	 RIT Below 161: Adds 1-digit to multiple-digit number with no regrouping Adds 1-digit to multiple-digit number with regrouping Adds two 1-digit numbers with sums to 10 in horizontal format Uses models to calculate whole number sums through 99 Uses models to construct whole number addition facts with addends through 10